BIOLOGICAL SCALING Does the exception prove the rule?

Arising from: P. B. Reich, M. G. Tjoelker, J.-L. Machado & J. Oleksyn Nature 439, 457-461 (2006)

Reich *et al.*¹ report that the whole-plant respiration rate, *R*, in seedlings scales linearly with plant mass, *M*, so that $R = c_R M^{\theta}$ when $\theta \approx 1$, in which c_R is the scaling normalization and θ is the scaling exponent. They also state that because nitrogen concentration (*N*) is correlated with c_R variation in *N* is a better predictor of *R* than *M* would be. Reich *et al.* and Hedin² incorrectly claim that these "universal" findings question the central tenet of metabolic scaling theory, which they interpret as predicting $\theta = \frac{3}{4}$, irrespective of the size of the plant. Here we show that these conclusions misrepresent metabolic scaling theory and that their results are actually consistent with this theory.

Reich et al. and Hedin do not cite an explicit caveat in metabolic scaling theory that θ will deviate from ³/₄ in plants that violate the secondary optimizing assumptions, including small plants such as seedlings and saplings^{3,4}. The core assumption^{3,5} of this theory states that carbon assimilation by the whole plant, or gross photosynthesis, P, stem fluid flow rate, Q_0 , and that the number (n_1) and mass of leaves $(M_{\rm L})$ all co-vary and scale together, as $R \propto P \propto Q_0 \propto n_{\rm L} \propto M_{\rm L} \propto M^{\theta}$, in which θ is derived from vascular network geometry, dynamics and biomechanics. Specifically, $\theta = 1/(2a + b)$, in which *a* characterizes the branch radii, r, between different branching levels, k (that is, k: $r_{k+1}/r_k \equiv n^{-a}$); b characterizes the ratio of branch lengths, *l*, between levels (that is, $l_{k+1}/l_k \equiv n^{-b}$)^{3,5}; and *n* is the branching ratio. The $\theta = \frac{3}{4}$ rule then originates from secondary assumptions³, whereby the branching network is volume-filling; hydrodynamic resistance is minimized; the terminal branch (that is, M_L , R_L , P_L , Q_L) is independent of *M*; and biomechanical adaptations negate the effects of gravity. Together, these assumptions lead to $a = \frac{1}{2}$, $b = \frac{1}{3}$, and consequently, $\theta = \frac{3}{4}$. Violations of any of these assumptions yield different values⁶ of *a* and/or *b*, and hence of θ .

Isometric scaling relationships for small plants are the result of such violations. For small plants, gravity is relatively unimportant, so $r_k \approx l_k$ and $a \approx \frac{1}{3}$, rather than $a = \frac{1}{2}$ (Fig. 1a). Also, there are few branching levels, so space-filling is incomplete and $b > \frac{1}{3}$. Thus, metabolic scaling theory predicts that $\theta \approx 1$ for the extreme case of very small plants. However, as plants grow, gravity becomes increasingly important and volume-filling architecture develops³, so metabolic scaling theory predicts a shift in θ from ≈ 1 to $\sim \frac{3}{4}$ (Fig. 1b).

Independent data sets support these predictions. First, intraspecific scaling of metabolism⁷ from saplings to trees is closer to ³/₄ than to 1. Second, intra- and interspecific scaling of M_L all show⁴ a transition from $\theta \approx 1$ in seedlings to $\theta \approx ³/₄$ in larger plants (Fig. 1b). Furthermore, the data of Reich *et al.* for *R* show a shift from $\theta \approx 1$ for seedlings to $\theta \approx ³/₄$ for saplings that



Figure 1 | **Metabolic scaling theory (MST) predicts a coordinated shift in allometric exponents. a,** Interspecific scaling for branch diameters $(2 \times r)$ and lengths (l) from seedlings to trees¹⁵. As predicted, the scaling exponent changes from ≥ 1 for small plants and seedlings (green squares, above-ground biomass < 1 g, reduced major axis (RMA) fit, $b/a = 1.8 \pm 0.12$; see text) to $b/a = 0.97 \pm 0.048$ for all the larger plants (red and brown diamonds; RMA fit not shown) to $\sim \frac{3}{2}$ (RMA fit, $b/a = 0.65 \pm 0.02$) for the maximum interspecific heights achieved¹⁵ (brown diamonds). **b**, As the scaling of branch lengths and radii changes, the scaling of total leaf biomass¹², M_I , as well as R and P, are then all predicted to change. Indeed, $\theta = 1.01 \pm 0.7$ (n = 95, $r^2 = 0.88$) for plants with a mass of < 1 g and $\theta = 0.77 \pm 0.2$ for plants with a mass of > 1 g (n = 563, $r^2 = 0.959$), which is consistent with the MST-predicted shift from $\theta = 1$ to $\theta = \frac{3}{4}$ and the scaling relationships in **a**.



Figure 2 | Plant carbon growth. This is represented by G = P - R, in which $P = P_L M_L$, and P_L is the rate of assimilation. Metabolic scaling theory (MST) predicts that $M_{\rm L} = c_{\rm L} M^{\frac{3}{4}}$ for plants larger than seedlings. Given that $c_{\rm L} \approx 0.7 \, {\rm g}^{\frac{1}{4}}$ (Fig. 1b) and that the geometric mean¹⁰ of $P_{\rm L}$ (95.5 nmol C $g^{-1} s^{-1}$) yields $P \approx 67 M^{\frac{5}{4}}$ (nmol C $g^{-\frac{5}{4}} s^{-1}$), Reich *et al.* claim that, within treatments, $R = c_R M^{\theta}$, in which $\theta \approx 1$ and $c_R \approx 24$ nmol C g⁻¹ s⁻¹. Thus, $G = P - R \approx 67M^{\frac{3}{4}} - 24M \text{ (nmol C s}^{-1}\text{). Growth}$ ceases when $G \rightarrow 1$ (and P = R), yielding the erroneous prediction of an unrealistic maximum size (curved black line) of ~1 kg. The red line $(G \approx 67M^{\frac{3}{4}} - 24M^{\frac{3}{4}})$, in which c_2 has units of nmol C g^{-3/4} s⁻¹, is for plants larger than seedlings when $\theta = \frac{3}{4}$, as predicted by MST (Fig. 1b). Note that, as discussed^{13,14}, the potential variation in c_1 and c_p is influenced by nutrient stoichiometry. These results show that isometric scaling within individual experiments cannot continue as plants grow larger than seedlings.

have an above-ground biomass of more than $30 \text{ g} (\theta = 0.78 \pm 0.08, r^2 = 0.86).$

Reich *et al.* do not cite studies of plants larger than seedlings, which show the predicted $\frac{3}{4}$ power scaling for M_L (Fig. 1b), Q_0 , carbon growth rate (G = P - R), and chlorophyll concentration^{6,8}. Thus, within each of their experimental treatments, extrapolation of isometric scaling of R to plants larger than seedlings will erroneously predict that the ratio of R/G should increase, as $R/G \propto M^1/M^{\frac{5}{4}} = M^{\frac{5}{4}}$, and an unrealistic maximum plant size (Fig. 2). Metabolic scaling theory resolves these inconsistencies³ by showing that $R \propto P \propto Q_0 \propto n_L$ so that R/Gis invariant with size from seedlings to trees, as observed⁹.

Reich *et al.* point to the correlation between R and N as an alternative scaling mechanism. This is problematic and misleading. First, the literature¹⁰ on leaf-level physiology shows that $R \propto N$ cannot be assumed to apply to whole plants. Nitrogen is present, in varying concentrations, in all structures¹¹, so it is unclear how

N scales. As size increases, the metabolically inert pith and heartwood constitute an increasing fraction of biomass¹², but the fraction of nitrogen-rich leaves decreases as M^{-4} . Second, work extending metabolic scaling theory^{13,14} anticipated their result by showing how variation in nutrients influence *R* and related rates by changing the intercept of the predicted c_R , as observed¹.

For both plants and animals, metabolic scaling theory provides a general mechanistic baseline theory to predict how the scaling of metabolism is linked to the geometry and scaling of branching vascular networks, θ , temperature and nutrient stoichiometry — that is, nitrogen concentration. As a result, metabolic scaling theory can successfully resolve apparent exceptions and deviations^{3,6}, including isometric scaling in seedlings.

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Reich et al. reply

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Enquist *et al.*¹ raise several points that they claim cast doubt on our findings and interpretation² regarding whole-plant relations of respiration, *R*, with plant mass, *M*, and total plant nitrogen content, *N*. We agree with Enquist *et al.* that *R* does not scale isometrically with *M* across all plants. However, their assertion that we claim that isometric scaling $(R \propto M^{\theta}, \text{ with } \theta = 1)$ is universal in plants of all sizes is incorrect — in fact, we conclude the opposite², noting that there is isometric scaling within individual experiments, non-isometric scaling of respiration versus mass across all data pooled, and no common relation across all data².

Enquist *et al.*¹ also claim that isometric scaling is evident only for very small seedlings that have a dry mass of less than 3 g (for example, see their Fig. 1b), but that leaf mass in larger plants is proportional to $M^{\frac{3}{4}}$ and $R \propto M^{\frac{3}{4}}$. By contrast, our results show that $R \propto M^{1.0}$ for plants ranging from 0.01 to 50 g, and from 1 to 1,000 g, within individual studies (Fig. 1a in ref. 2) and that there are significant differences in the intercepts of these relationships². Thus, $\theta < 1$ for all plants pooled and differs in individual studies, such that no single $R \propto M$ scaling model can apply, whereas $R \propto N^{1.0}$ reconciles all such differences². Enquist *et al.*¹ also criticize us for not noting their earlier suggestion³ that θ might deviate from $\theta = \frac{3}{4}$ for small plants, although they themselves predicted 3/4 metabolic scaling in plants of all sizes³⁻⁵.

The allometry presented in Fig. 1 of Enquist *et al.*¹ does not address our findings, which

directly test their prediction³⁻⁵ that $R \propto M^{\frac{3}{4}}$. These allometric relations are not equivalent to measures of plant metabolism and are, at best, only indirectly relevant. Irrespective of its relevance to scaling, Enquist et al. claim that allometric relations (their Fig. 1) for leaf $M \propto$ total M^{θ} show isometric scaling for seedlings of less than 1 g and $\theta \approx \frac{3}{4}$ for larger plants, although their Fig. 1 shows a θ that changes continuously across the entire gradient of size. As noted previously in a critique⁶ of the works of West, Brown and Enquist, arbitrary data parsing such as in Fig. 1 of Enquist *et al.*¹ can lead to widely varying θ values: for instance, in their Fig. 1b, leaf $M \propto \text{total } M^{\theta} \text{ has } \theta \approx 0.70$ for plants of less than 1,000 g (n = 334), 1.10for plants from 50,000 to 500,000 g (n = 158), and 2.20 for plants of more than 1,000,000 g (n = 25). Furthermore, an empirical study⁷ of leaf to whole-tree allometry for large trees showed that θ could vary from much lower than ³/₄ to much more than 1.0 depending on the nature of the data set, further refuting any notion of a constant allometry of leaf M to total plant M following ³/₄ scaling rules.

Nonetheless, the work by Enquist and colleagues has stimulated the field by providing testable predictions³, such as a universal $R \propto M^{4}$ relationship⁴. The plant data of Gillooly *et al.*⁴ (n = 20) were mostly for fruits or tubers (not plants) such as bananas, lemons, strawberries and carrots, with data on *R* and *M* obtained from unrelated sources. Given the general importance of this predicted relationship, including in subsequent synthesis and

modelling by this group^{5,8}, we tested it using a comprehensive data set² that included coupled whole-plant mass and respiration measures. Those data do not support predictions of a universal $R \propto M^{\frac{3}{4}}$ scaling in plants.



Figure 1 | Evidence for positive carbon balance across all plant sizes. a, b, Estimated maximum 24-hour net carbon balance in relation to total plant mass (a) and total plant nitrogen (b) for the plants in ref. 2. The 24-hour net carbon balance is based on predicting light-saturated rates of net photosynthesis from photosynthesis-nitrogen relationships¹¹, and scaling carbon gain and respiratory carbon loss to the whole plant based on tissue nitrogen and biomass distribution.